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**Fatigue life prediction  
of small notched Ti-6AL-4V  
based on the theory of critical distance**

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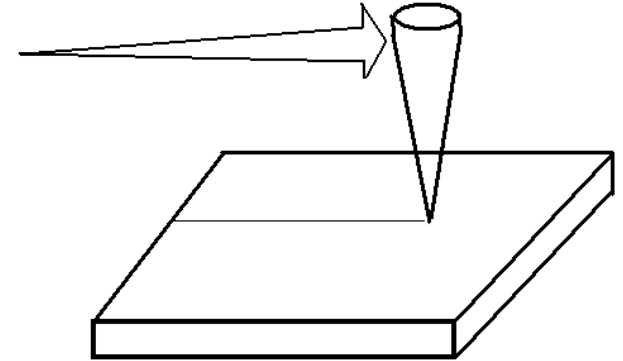
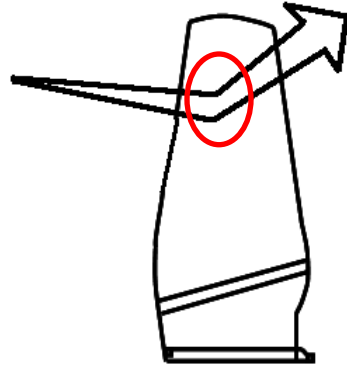
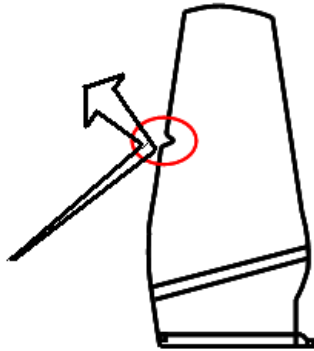
**IHI**

- 1 Background and objective
- 2 Experiment
- 3 Application of conventional theory of critical distance (TCD)
- 4 SEM observation
- 5 Appropriate method for determination of critical distance stress
- 6 Minimum fatigue strength of small notched Ti-64
- 7 Discussion of residual stress effects on FOD-HCF
- 8 Conclusions



Ref: Nicholas(2004), 10th National Turbine Engine HCF Conference New Orleans

- FOD may result in “nick”, “dent” and “scratch” at the leading edges of airfoils which in turn, reduce the fatigue strength of the material.
- FOD-induced HCF is one of the significant themes in fatigue problems of aero-engine component.
- Small notch effects on fatigue strength should be taken into account.



**Nick**

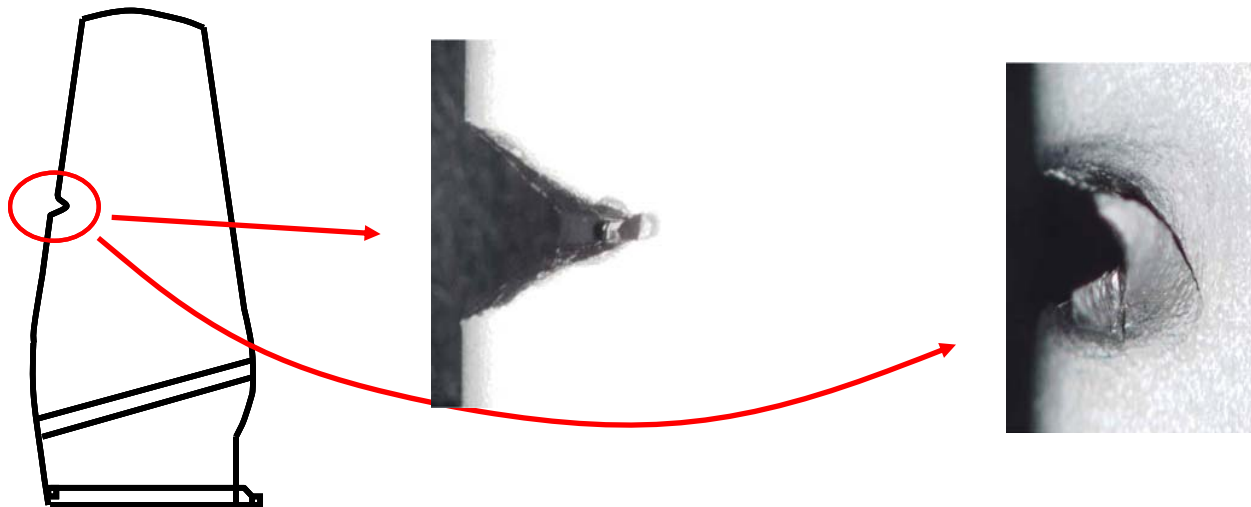


**Dent**



**Scratch**

- To investigate the method for fatigue life prediction of small notched Ti-64 specimens using the theory of the critical distance (TCD)
- To construct the appropriate method to evaluate fatigue life of Ti-64 with various notch radii and notch depths from the relationships between the critical distance stress and fatigue crack initiation life



**fan blade**

**small FOD damage**

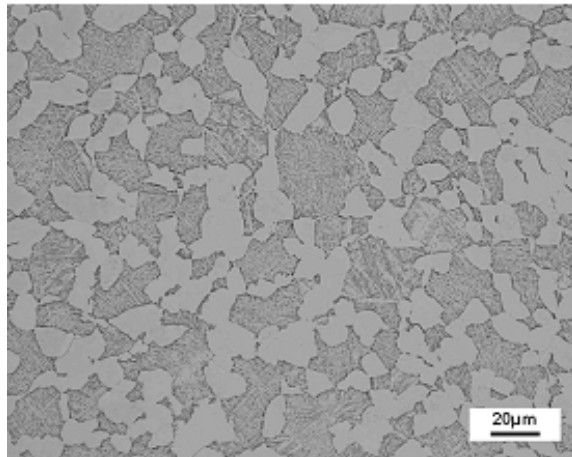
**FOD damage at leading edge of airfoil**

## Chemical composition of Ti-64 (mass %).

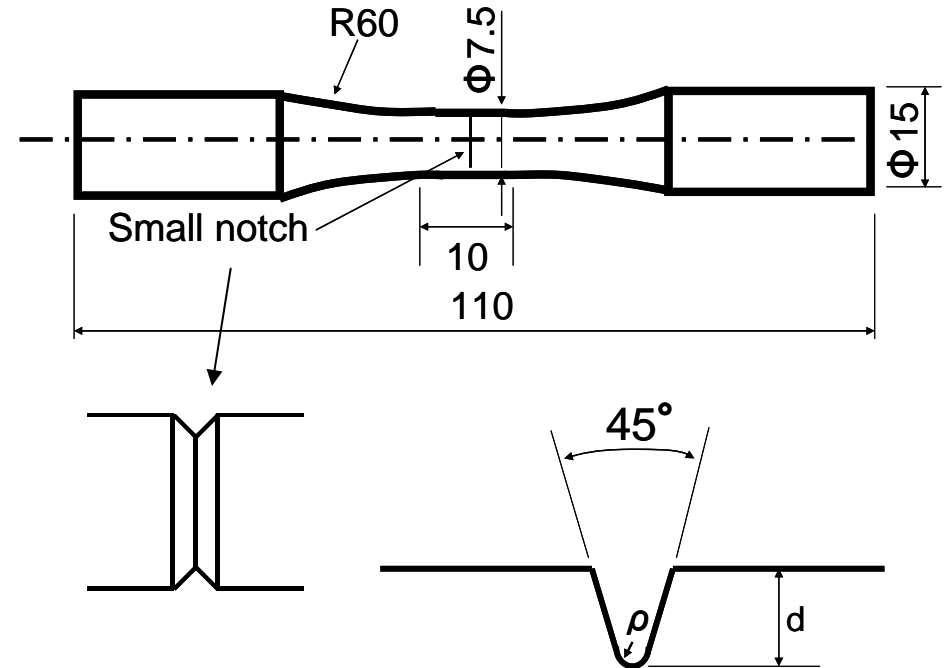
C	V	Al	Ti	N	Fe	O	H
0.002	4.16	6.3	bal.	0.004	0.16	0.2	0.0053

## Mechanical properties of Ti-64.

$\sigma_{Y0}$ (MPa)	$\sigma_{uts}$ (MPa)	$\epsilon_f$ (%)	$\psi$ (%)	$E$ (GPa)
935	1006	18.4	44.5	110



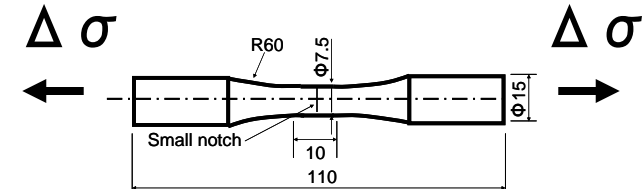
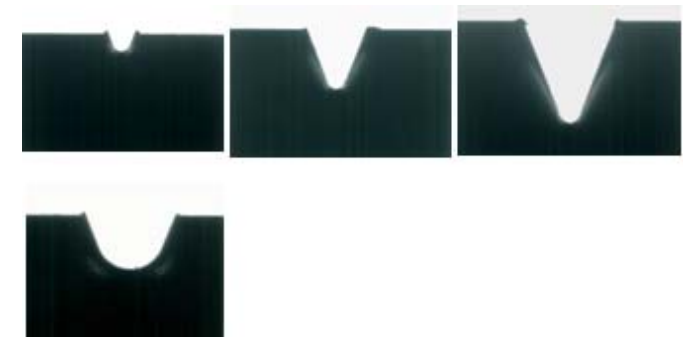
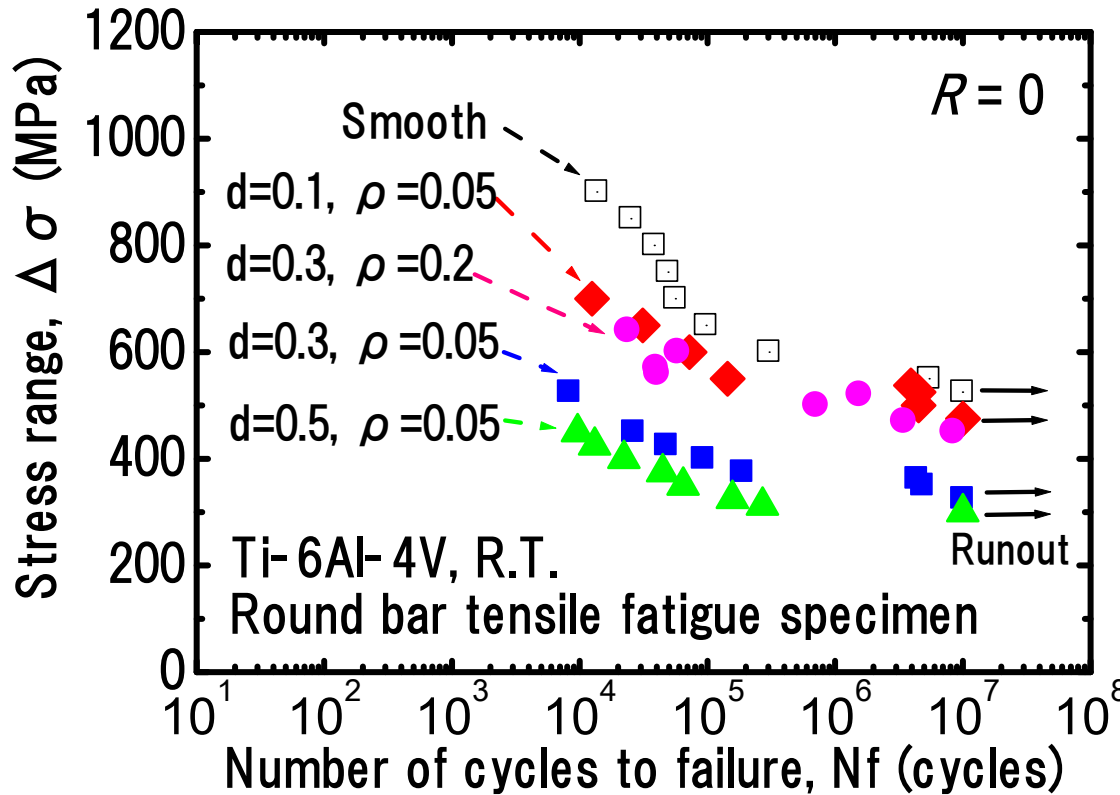
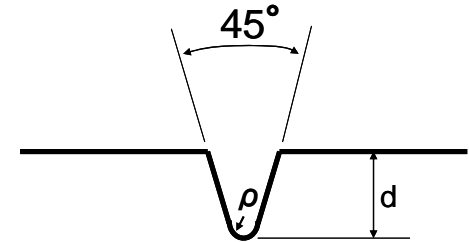
**Bimodal microstructure of Ti-64 (STOA)**

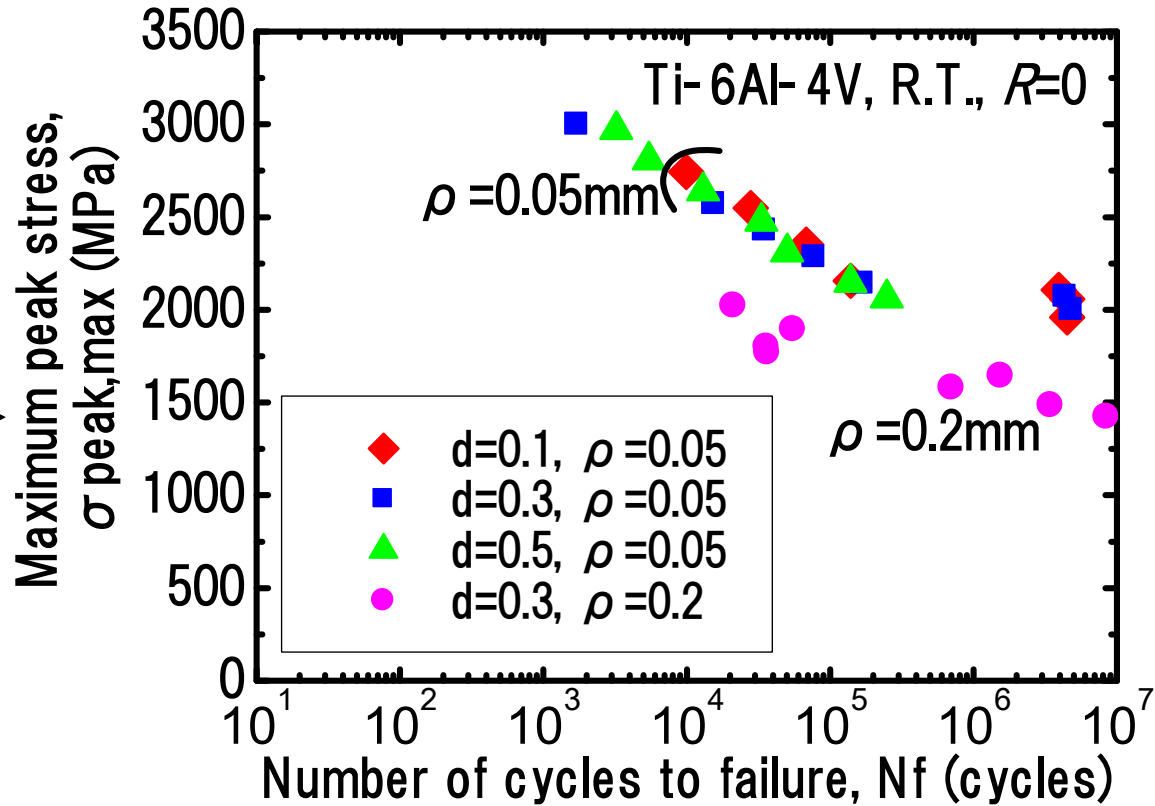
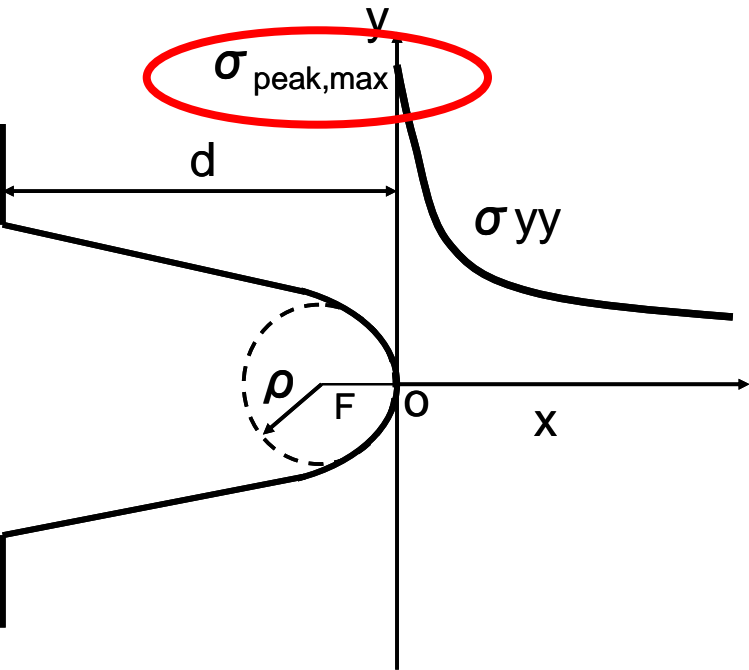


**Circumferential notch**

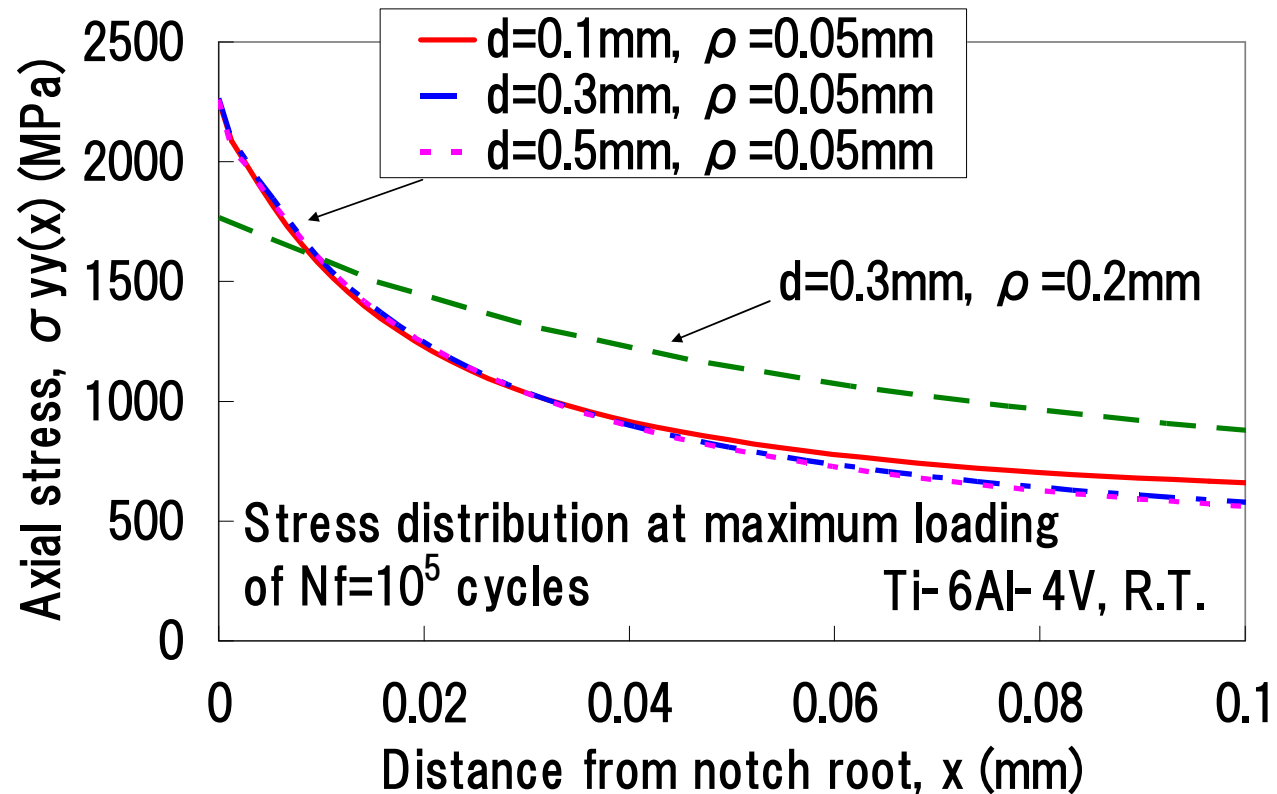
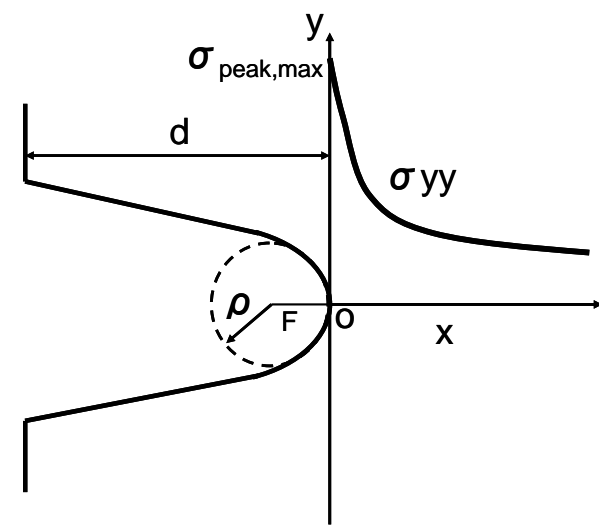
## Fatigue test conditions (0-tension, $R=0$ ).

Notch depth, $d$ (mm)	Notch root radius, $\rho$ (mm)	Note
0	$\infty$	Smooth specimen
0.1	0.05	Notch specimen
0.3	0.05	Notch specimen
0.5	0.05	Notch specimen
0.3	0.2	Notch specimen



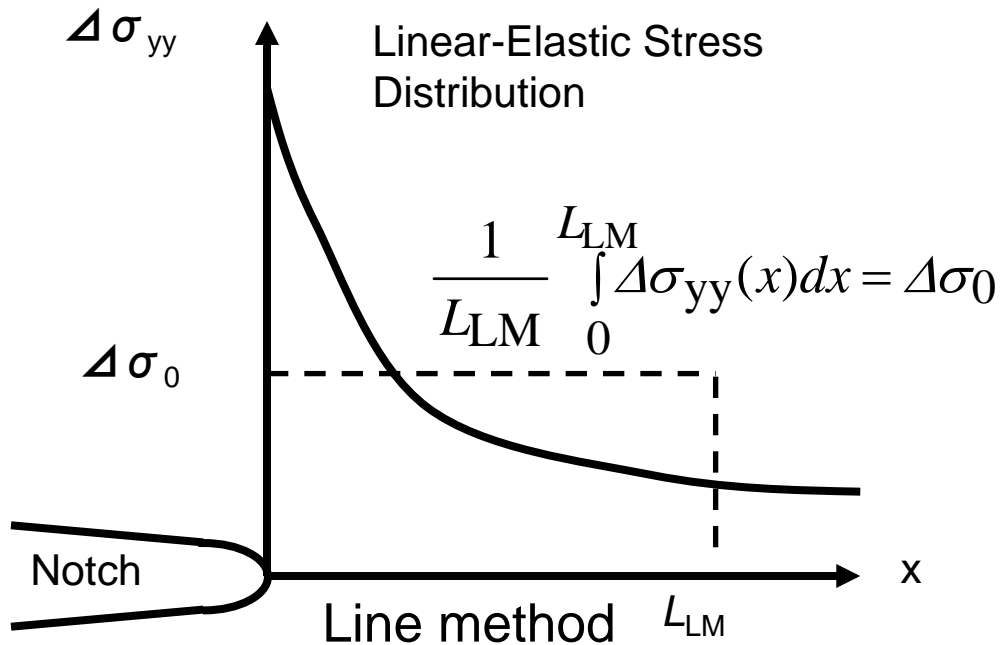


**Fatigue life prediction based on maximum peak stress approach gives inaccurate results for the notch fatigue life of various notch root radii.**



Comparison at the same life of  $N_f=1.0 \times 10^5$  cycles

Maximum peak stress at notch root and the stress gradient have to be taken into account in fatigue life prediction for small notched specimens.



The most simple approach conventionally determines the distance inward from the notch root to the location at which the average stress range of the notched specimen is equal to the stress range of smooth specimens at the same fatigue life.

Conventional TCD was proposed by :

Neuber: (1958) [4], Peterson: (1959) [5]

Tanaka: Int. J. of Fract. (1983) [13]

Taylor: Eng. Fract. Mech. (2008) [6-8]

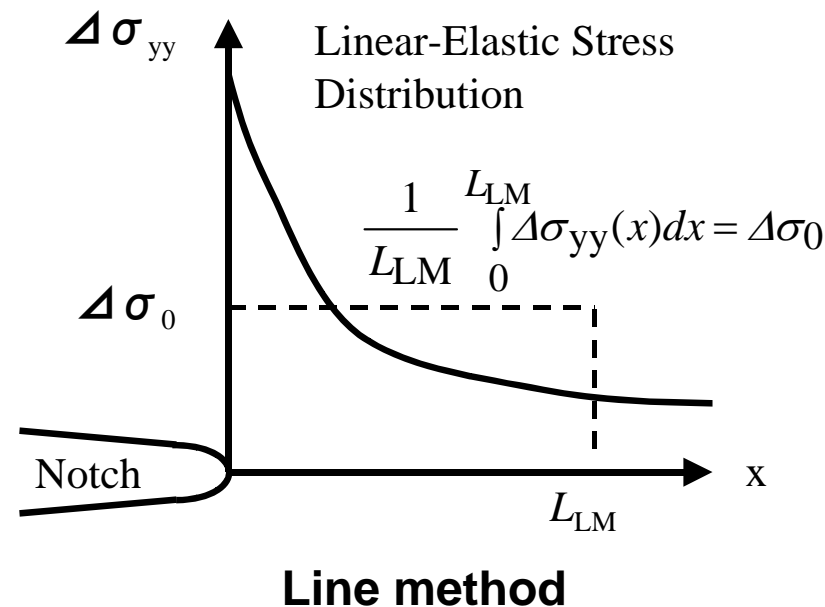
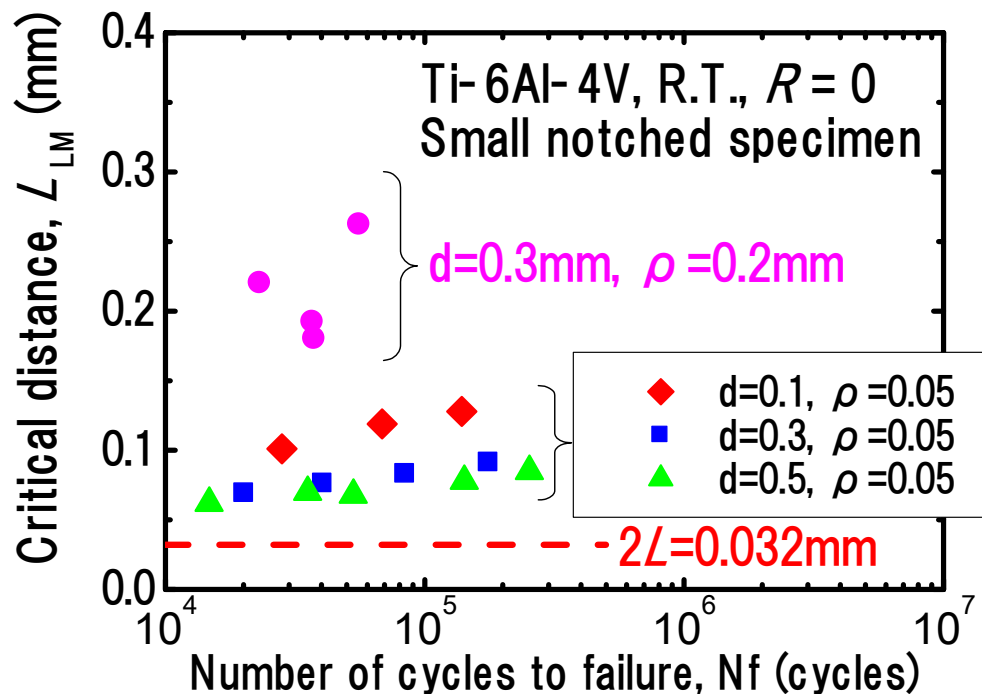
Line method  $LLM = 2L = 0.032\text{mm}$

$$L = \frac{1}{\pi} \left( \frac{\Delta K_{th}}{\Delta\sigma_0} \right)^2$$

$$\Delta\sigma_0 = 538\text{MPa}$$

$$\Delta K_{th} = 3.86\text{MPa}\sqrt{\text{m}}$$

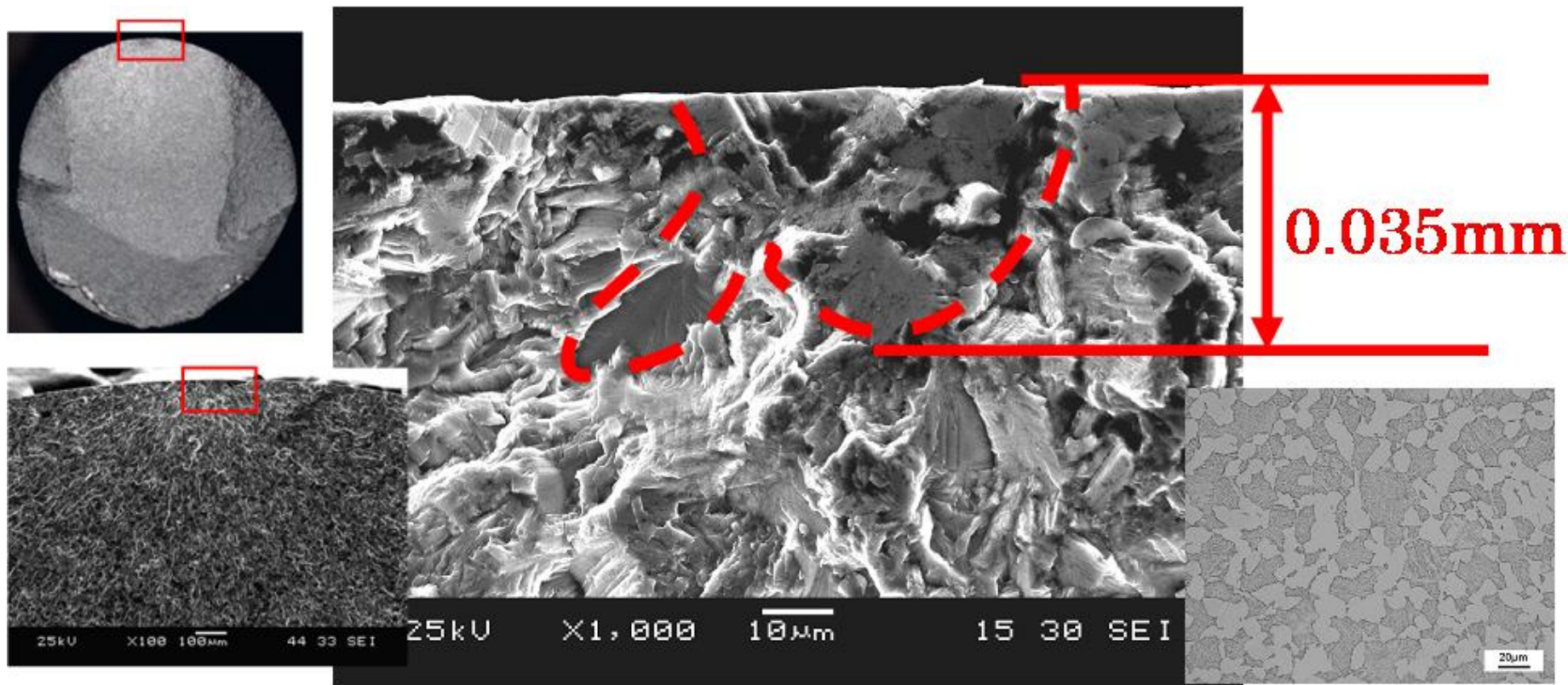
NASA / NASGLO



The critical distances for  $\rho = 0.2\text{mm}$  are larger than those for  $\rho = 0.05\text{mm}$ .

The conventional TCD approach may not give an appropriate unified value, when the notch tip radius of the notched specimens is different from each other.

$L_{LM}=2L$  of the line method of determination of the critical distances are much smaller than the critical distances as the distance inward from the notch root to the location at which the stress range required for a fatigue failure life is equal to the stress range required for the same fatigue failure life for smooth specimens.



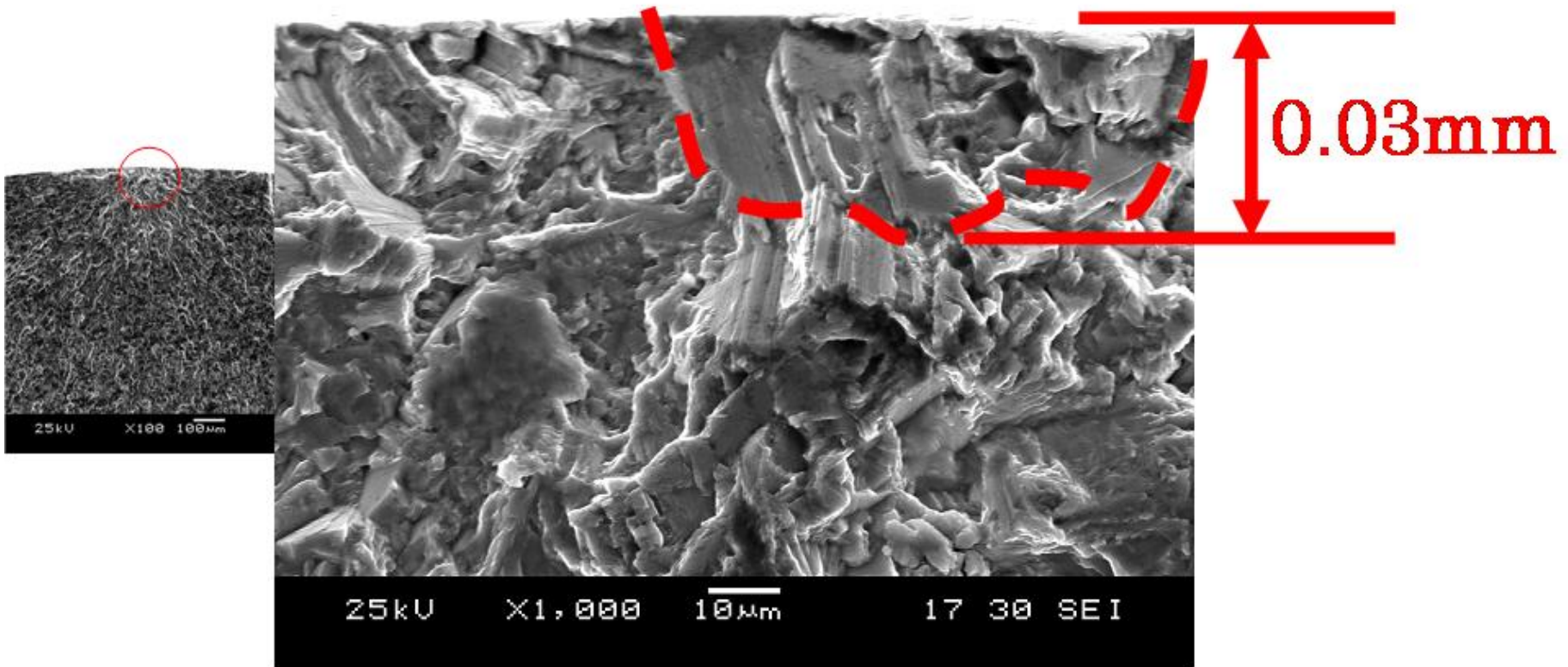
Smooth specimen of  $N_f=5.67 \times 10^4$

## Fatigue crack initiation site

→quasi-cleavage, **crystallographic facets at origin**, no inclusion

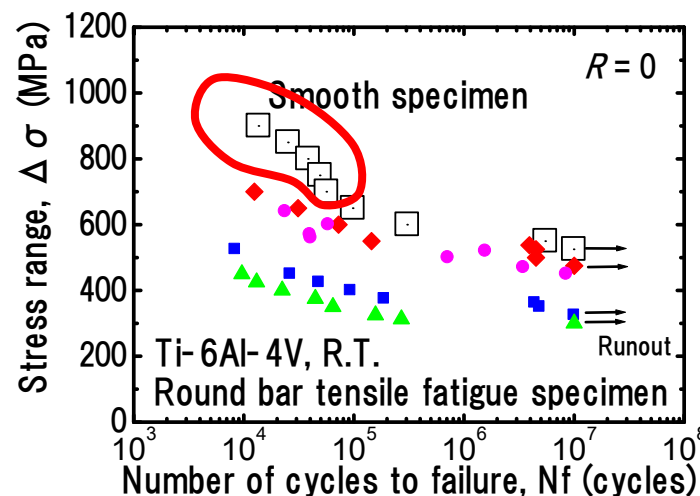
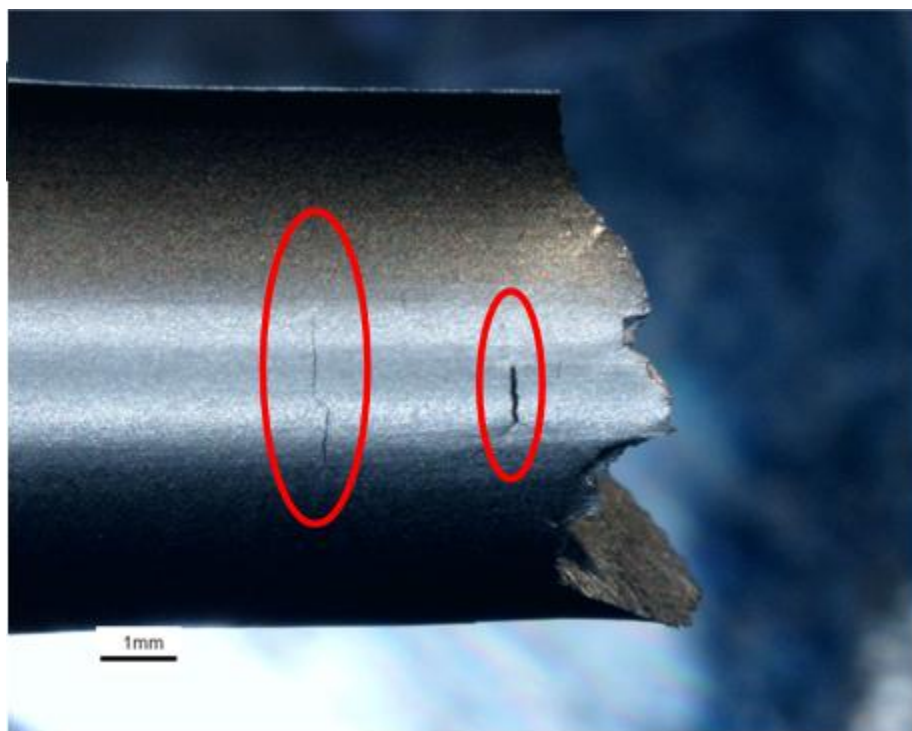
The facets :  $\alpha$  phase (A. Nozue [17], H. Oguma [18], O. Jin [19]),

**approximately semi-circle, equal to average  $\alpha$  phase size**

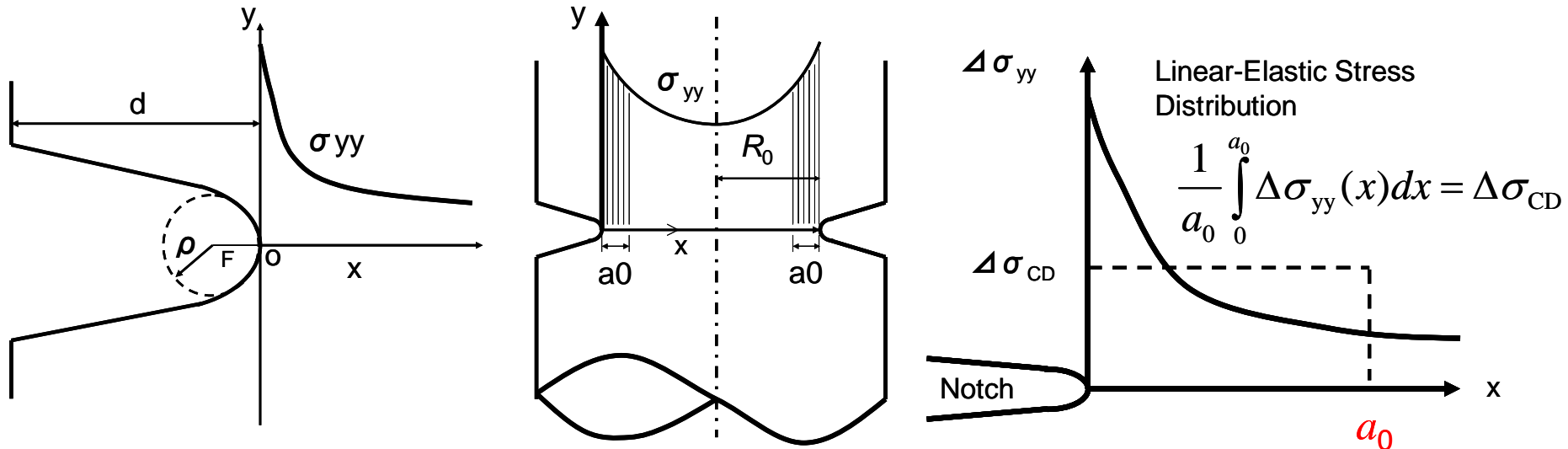


Smooth specimen of  $N_f=3.86 \times 10^4$

The determination procedure of the critical distance calculated from  $\Delta K$  equation of semi-circle crack is appropriate for the forged Ti-64.



- ✓ The volume effects of fatigue fracture process zone extend throughout the gauge length of 10mm.
- ✓ Difference in volume effects between the notched and smooth specimen
- ✓ This is the evidence that the approach in determination of the critical distance, as the distance inward from the notch root to the location at which the stress range is equal to the stress range of smooth specimens, does not give an appropriate unified value.



**Method (1) : K eq. of through crack in infinite plate (0.016mm)**

$$a_0 = (1/\pi) \cdot (\Delta K_{th} / \Delta \sigma_0)^2 \quad \because \Delta K = \Delta \sigma \sqrt{\pi a}$$

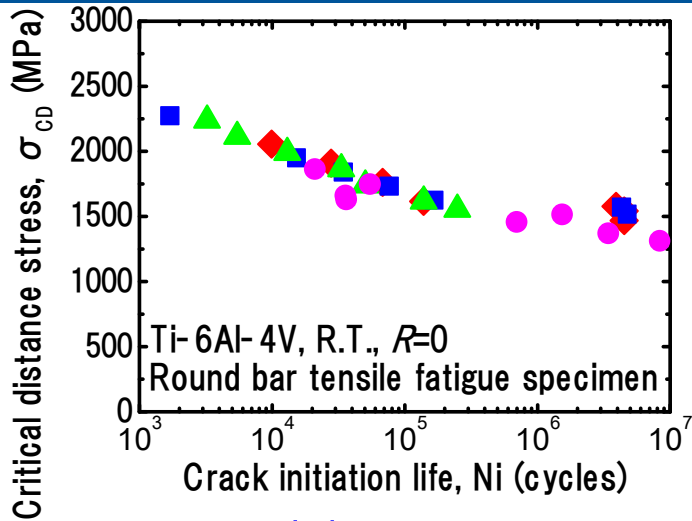
**Method (2) : K eq. of semi-circle surface crack (0.032mm)**

$$a_0 = (1/\pi) \cdot (\pi \cdot \Delta K_{th} / (1.1215 \times 2 \times \Delta \sigma_0))^2 \quad \because \Delta K = 1.1215 \cdot (2/\pi) \cdot \Delta \sigma \sqrt{\pi a}$$

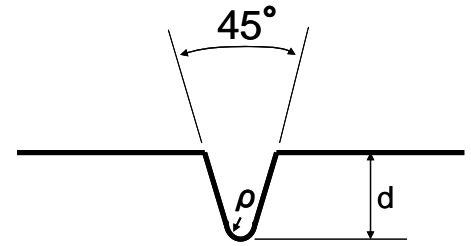
**Critical distance stress : Average stress in fatigue fracture process zone**

$$\sigma_{CD} = \frac{\int_0^{a_0} \sigma_{yy}(x) \cdot 2\pi \cdot (R_0 - x) \cdot dx}{\int_0^{a_0} 2\pi \cdot (R_0 - x) \cdot dx}$$

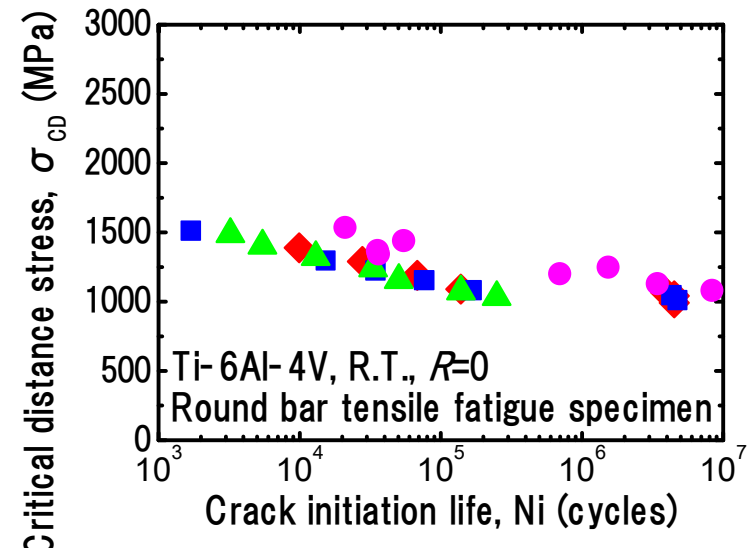
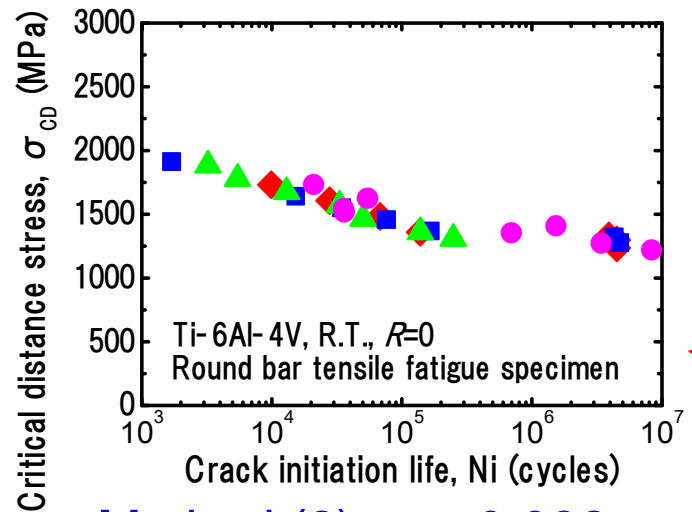
# Appropriate critical distance stress



- ◆  $d=0.1\text{mm}, \rho=0.05\text{mm}$
- $d=0.3\text{mm}, \rho=0.05\text{mm}$
- ▲  $d=0.5\text{mm}, \rho=0.05\text{mm}$
- $d=0.5\text{mm}, \rho=0.2\text{mm}$



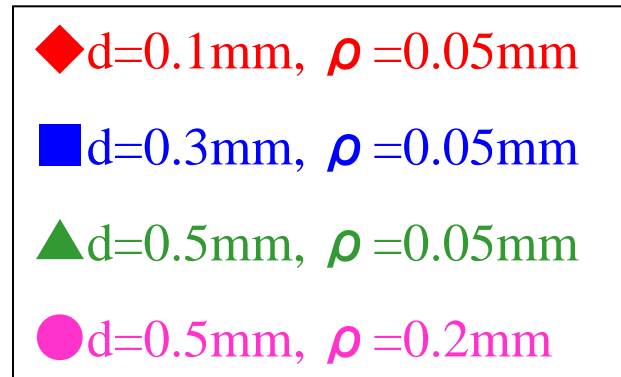
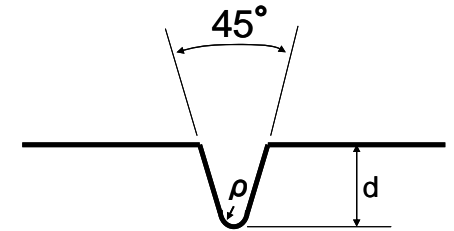
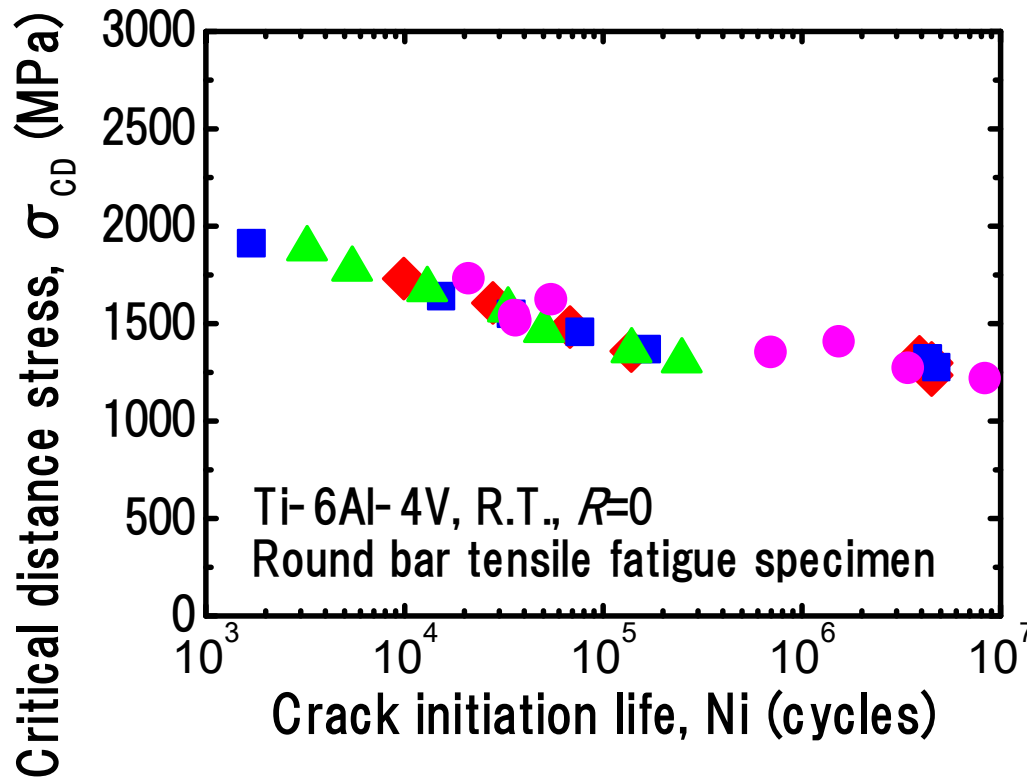
Method (1)  $a_0 = 0.016 \text{ mm}$   
 $a_0 = (1/\pi) \cdot (\Delta K_{th} / \Delta \sigma_0)^2$



(3)  $a_0 = 0.064\text{mm} = 0.032 \times 2 \text{ mm}$

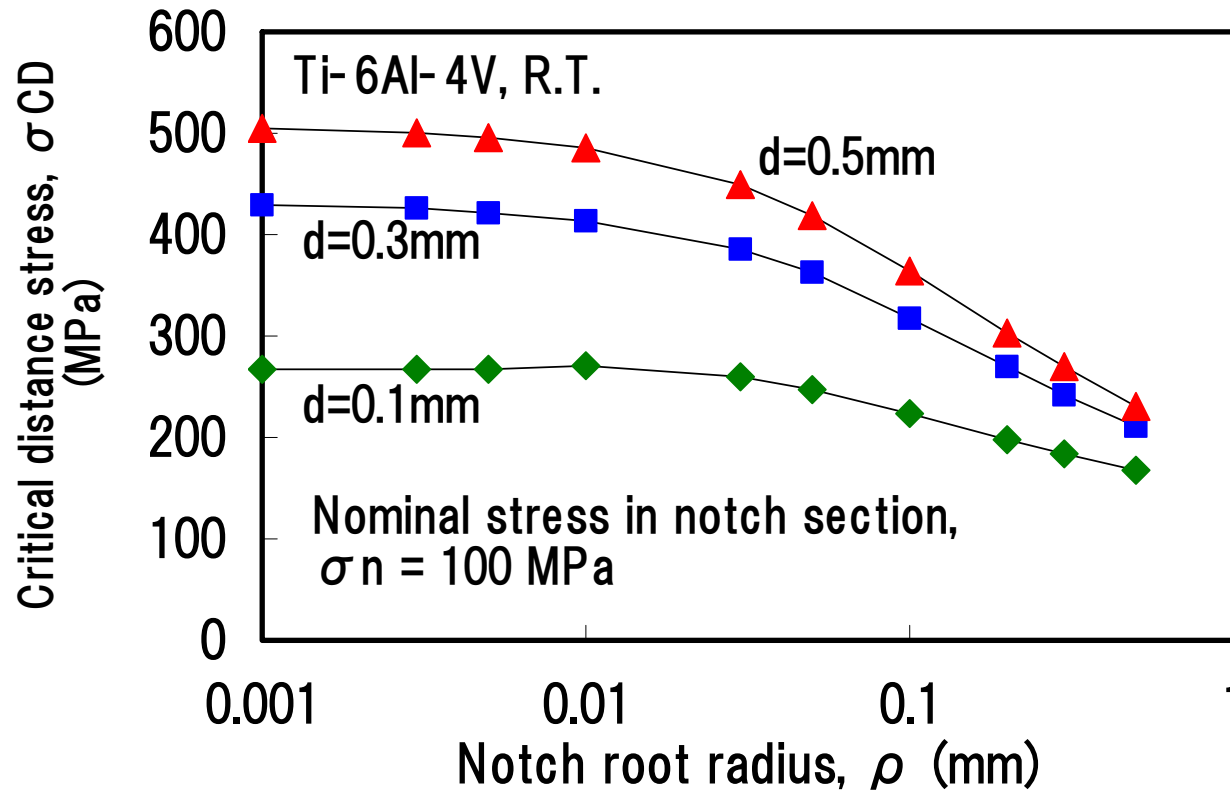
Best correlation for all fatigue test data

Method (2)  $a_0 = 0.032 \text{ mm}$   $a_0 = (1/\pi) \cdot (\pi \cdot \Delta K_{th} / (1.1215 \times 2 \times \Delta \sigma_0))^2$



$$a_0 = (1/\pi) \cdot (\pi \cdot \Delta K_{th} / (1.1215 \times 2 \times \Delta \sigma_0))^2$$

✓ There exists the good correlation between critical distance stress and crack initiation life of small notched specimen if the critical distance,  $a_0$ , is determined with  $10^7$  cycle  $\Delta \sigma_0$ , and  $\Delta K_{th}$  using the K equation of semi-circle surface crack.



Very small notch root radius of  $\rho=0.001-0.01$ mm gives the constant critical distance stress at the same fatigue initiation life.

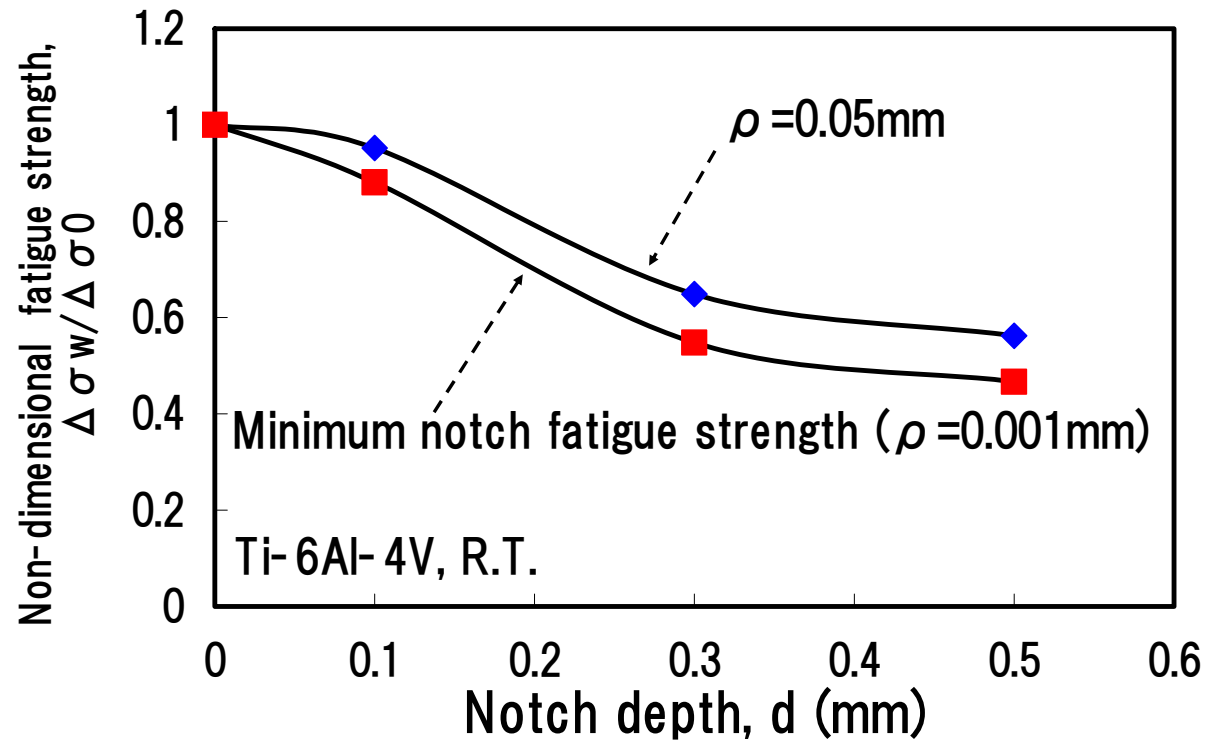
Minimum notch fatigue strength exists for each notch depth of  $d=0.1, 0.3$  and  $0.5$ mm.

$\Delta \sigma_w$

:  $10^7$  notch fatigue strength

$\Delta \sigma_0$

:  $10^7$  smooth specimen fatigue strength



■ : minimum fatigue reduction curve ( $\rho = 0.001\text{mm}$ ) can be determined by the appropriate critical distance stress

The design engineer can determine the minimum fatigue strength of the airfoils with nicks, dents and scratches in fatigue strength design of the airfoils.

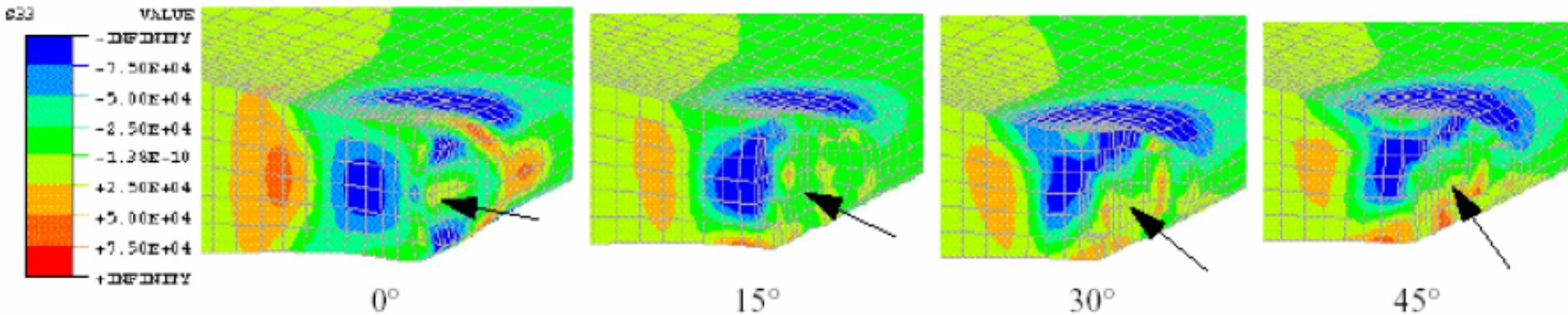
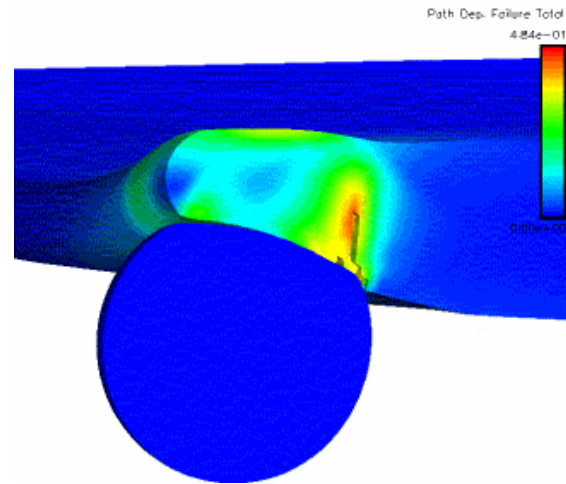
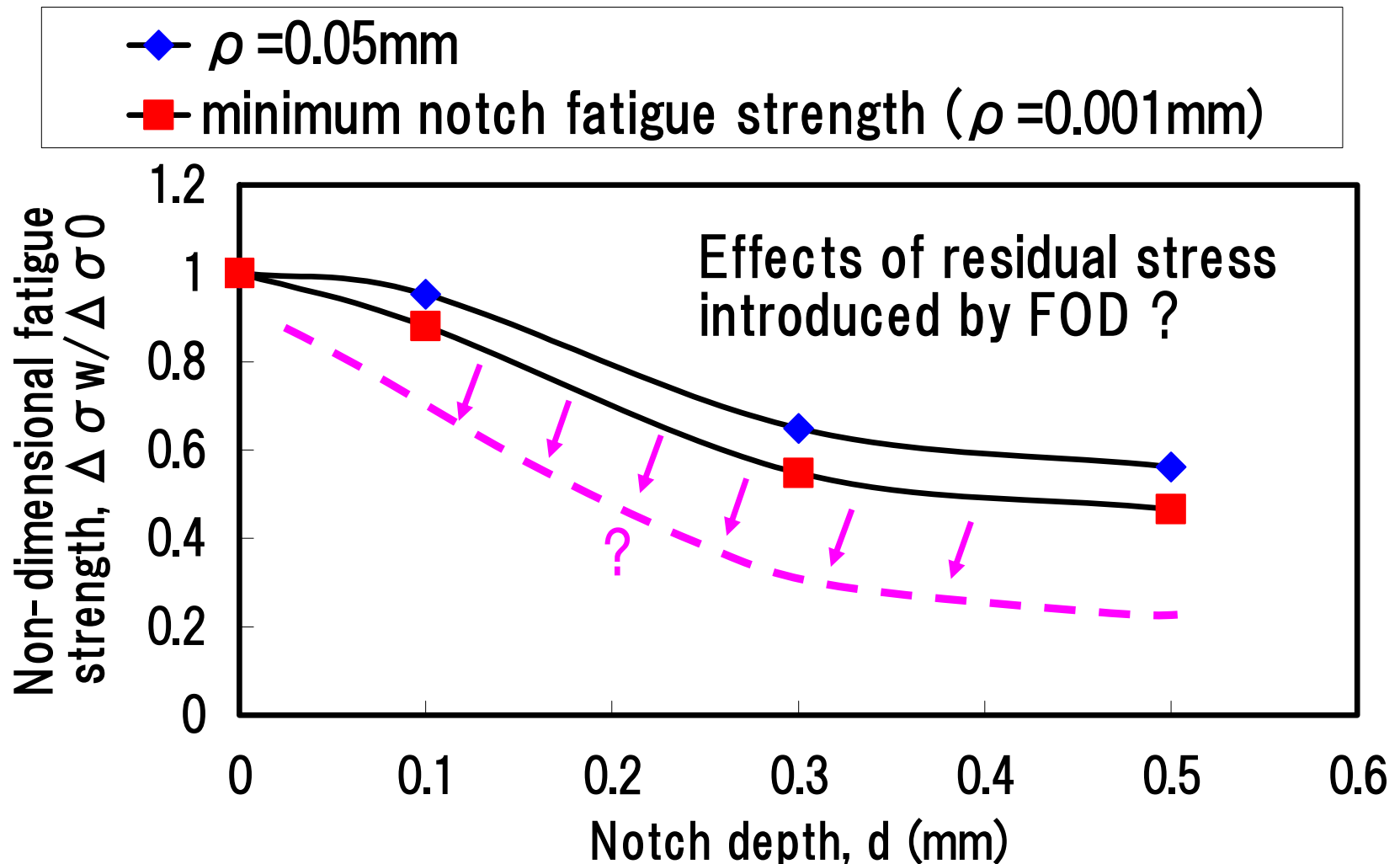


Figure 36: Comparison of Residual Stress Fields for Different Impact Angles.

## Example of FOD simulation

Ref. The Research and Technology Organisation (RTO) of NATO, RTO technical report, TR-AVT-094 (2007) 78-84.



✓ Residual stress effects may be needed to take into account to evaluate the FOD-induced HCF.

## Small notched fatigue strength based on the appropriate TCD for Ti-64

- ✓ There exists the good correlation between critical distance stress and crack initiation life when the critical distance,  $a_0$ , was determined with plain fatigue limit,  $\Delta\sigma_0$ , and  $\Delta K_{th}$  using the K equation of semi-circle surface crack.
- ✓ The critical distance approach is powerful engineering tool to determine the small notched minimum fatigue strength under a required fatigue life in design if it is appropriately applied.

## ACKNOWLEDGEMENTS

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**Thank You  
for Attention.**